

$$\begin{aligned}
 1. \quad & \frac{x^2 y - y^3}{x^2 - 2xy + y^2} : \frac{x^2 + 2xy + y^2}{x^3 - xy^2} = \\
 & = \frac{y(x^2 - y^2)}{(x - y)^2} : \frac{(x + y)^2}{x(x^2 - y^2)} = \frac{y(x - y)(x + y)}{(x - y)^2} \cdot \frac{x(x - y)(x + y)}{(x + y)^2} = xy
 \end{aligned}$$

c.a.: $x \neq 0$; $x - y \neq 0$; $x + y \neq 0$

$$\begin{aligned}
 2. \quad & \left(\frac{1}{2a - 1} - \frac{1}{2a + 1} \right) : \left(\frac{b}{2a - 1} + \frac{b}{2a + 1} \right) = \\
 & = \frac{2a + 1 - (2a - 1)}{(2a - 1)(2a + 1)} : \frac{b(2a + 1) + b(2a - 1)}{(2a - 1)(2a + 1)} = \\
 & = \frac{2a + 1 - 2a + 1}{(2a - 1)(2a + 1)} : \frac{2ab + b + 2ab - b}{(2a - 1)(2a + 1)} = \\
 & = \frac{2}{(2a - 1)(2a + 1)} \cdot \frac{(2a - 1)(2a + 1)}{4ab} = \frac{1}{2ab}
 \end{aligned}$$

c.a.: $a \neq 0$; $b \neq 0$; $2a + 1 \neq 0$; $2a - 1 \neq 0$

$$\begin{aligned}
 3. \quad & \frac{x^2 - 1}{x} - \frac{x^2}{x + 1} + \frac{1}{x^2 + x} - \frac{x - 1}{x + 1} = \\
 & = \frac{x^2 - 1}{x} - \frac{x^2}{x + 1} + \frac{1}{x(x + 1)} - \frac{x - 1}{x + 1} = \\
 & = \frac{(x^2 - 1)(x + 1) - x^3 + 1 - x(x - 1)}{x(x + 1)} = \frac{x^3 + x^2 - x - 1 - x^3 + 1 - x^2 + x}{x(x + 1)} = 0
 \end{aligned}$$

c.a.: $x \neq 0$; $x + 1 \neq 0$

$$\begin{aligned}
 4. \quad & \left(2 + \frac{x^2 + y^2}{xy} \right)^2 \cdot \left[\frac{x - y}{x + y} + \frac{y^2}{(x + y)^2} \right]^2 : \frac{x^2}{y^2} = \\
 & = \left(\frac{2xy + x^2 + y^2}{xy} \right)^2 \cdot \left[\frac{x^2 - y^2 + y^2}{(x + y)^2} \right]^2 \cdot \frac{y^2}{x^2} = \\
 & = \left(\frac{(x + y)^2}{xy} \right)^2 \cdot \left[\frac{x^2}{(x + y)^2} \right]^2 \cdot \frac{y^2}{x^2} = \frac{(x + y)^4}{x^2 y^2} \cdot \frac{x^4}{(x + y)^4} \cdot \frac{y^2}{x^2} = 1
 \end{aligned}$$

c.a.: $x \neq 0$; $y \neq 0$; $x + y \neq 0$

$$\begin{aligned}
 5. \quad & 1 + y \cdot \left[\frac{5}{6y} + \frac{x}{3y^2 - 2x^2} \cdot \left(\frac{2x + y}{2x} - \frac{x + 3y}{3y} \right) \right] = \\
 & = 1 + y \cdot \left(\frac{5}{6y} + \frac{x}{3y^2 - 2x^2} \cdot \frac{3y(2x + y) - 2x(x + 3y)}{6xy} \right) = \\
 & = 1 + y \cdot \left(\frac{5}{6y} + \frac{x}{3y^2 - 2x^2} \cdot \frac{6xy + 3y^2 - 2x^2 - 6xy}{6xy} \right) = \\
 & = 1 + y \cdot \left(\frac{5}{6y} + \frac{x}{3y^2 - 2x^2} \cdot \frac{3y^2 - 2x^2}{6xy} \right) = 1 + y \cdot \left(\frac{5}{6y} + \frac{1}{6y} \right) = 1 + y \cdot \frac{6}{6y} = \mathbf{2}
 \end{aligned}$$

c.a.: $x \neq 0$; $y \neq 0$; $3y^2 - 2x^2 \neq 0$

$$\begin{aligned}
 6. \quad & \frac{1 + \frac{1}{xy}}{x - y} \cdot \left(x + \frac{1 - \frac{x}{y}}{\frac{1}{y} + x} \right) : \frac{\frac{1}{x^2} + 1}{1 - \frac{y}{x}} = \\
 & = \frac{xy + 1}{xy} \cdot \left(x + \frac{y - x}{\frac{1 + xy}{y}} \right) : \frac{\frac{1 + x^2}{x^2}}{\frac{x - y}{x}} = \\
 & = \frac{xy + 1}{xy} \cdot \frac{1}{x - y} \cdot \left(x + \frac{y - x}{y} \cdot \frac{y}{1 + xy} \right) : \left(\frac{1 + x^2}{x^2} \cdot \frac{x}{x - y} \right) = \\
 & = \frac{xy + 1}{xy(x - y)} \cdot \left(x + \frac{y - x}{1 + xy} \right) : \frac{1 + x^2}{x(x - y)} = \\
 & = \frac{xy + 1}{xy(x - y)} \cdot \frac{x + x^2y + y - x}{1 + xy} \cdot \frac{x(x - y)}{1 + x^2} = \\
 & = \frac{xy + 1}{xy(x - y)} \cdot \frac{y(x^2 + 1)}{1 + xy} \cdot \frac{x(x - y)}{1 + x^2} = \mathbf{1}
 \end{aligned}$$

c.a.: $x \neq 0$; $y \neq 0$; $1 + xy \neq 0$; $x - y \neq 0$